A R T I C L E S
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# Ab Initio Calculations of the Potential Surface for Rearrangement of 2,2,3,3-Tetrafluoromethylenecyclopropane to 1-(Difluoromethylene)-2,2-difluorocyclopropane 

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#### Abstract

CASSCF and CASPT2 calculations have been performed to understand the reason that addition of a second pair of geminal fluorines to methylenecyclopropane lowers the barrier to rearrangement by $6.7 \mathrm{kcal} / \mathrm{mol}$ more than addition of the first pair. Our calculations duplicate this experimental finding by Dolbier and co-workers. Our computational results confirm Dolbier's conjecture, that the non-additive lowering of $E_{\mathrm{a}}$ for the rearrangement of 2,2,3,3-tetrafluoromethylenecyclopropane (9) to 1-(difluoromethylene)-2,2difluorocyclopropane (11) is due to destabilization of 9 by the presence of the vicinal $\mathrm{CF}_{2}$ groups in this fluorocarbon. In the course of exploring the potential energy surface for the rearrangement of 9 , we have located a bond-stretch isomer (20) that differs from 9 by inversion of both $\mathrm{CF}_{2}$ groups. The enthalpy of 20 is computed to be $21.9 \mathrm{kcal} / \mathrm{mol}$ higher than that of 9 , but direct interconversion of these two "bond-stretch invertomers" requires passage over a TS whose enthalpy is calculated to be $11.7 \mathrm{kcal} / \mathrm{mol}$ higher than that of 20.


## Introduction

Geminal fluorine substitution profoundly affects the reactivity of cyclopropane. ${ }^{1}$ For example, the activation energy of $E_{\mathrm{a}}=$ $59.4 \mathrm{kcal} / \mathrm{mol}$ for cis-trans isomerization of 1,2-dimethylcyclopropane ${ }^{2}$ is reduced to $E_{\mathrm{a}}=49.7 \mathrm{kcal} / \mathrm{mol}$ in 1,1-difluoro-2,3-dimethylcyclopropane. ${ }^{3}$ Moreover, as predicted by ab initio calculations, ${ }^{4}$ the activation energy for racemization of optically active cis-1,1-difluoro-2-ethyl-3-methylcyclopropane is only $E_{\mathrm{a}}=41.3 \mathrm{kcal} / \mathrm{mol},{ }^{5} 16.5 \mathrm{kcal} / \mathrm{mol}$ lower than the activation energy for racemization of optically active cis-2-ethyl-3methylcyclopropane. ${ }^{6}$

Given the very large effects of geminal fluorine substitution on ring opening of cyclopropane, the finding by Dolbier and Fielder that $E_{\mathrm{a}}=38.3 \mathrm{kcal} / \mathrm{mol}$ for the methylenecyclopropane rearrangement of 2,2-difluoromethylenecyclopropane (1) to (difluoromethylene)cyclopropane (3) is lower by only about 2 $\mathrm{kcal} / \mathrm{mol}^{7}$ than the $E_{\mathrm{a}}$ for the rearrangement of the methyl-labeled hydrocarbon ${ }^{8}$ was quite surprising. Ab initio calculations revealed that this experimental finding is a consequence of the

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## Scheme 1


weakening of the $\pi$ bond to the $\mathrm{CF}_{2}$ group in the transition structure (TS), connecting $\mathbf{1}$ to diradical intermediate $\mathbf{2}$ (Scheme $1),{ }^{9}$ by the strong preference of difluorinated radical centers for pyramidal geometries. ${ }^{10}$

On the other hand, in the crypto methylenecyclopropane rearrangement of $\mathbf{1}$ to $\mathbf{5}$, via diradical intermediate $\mathbf{4}$, a $\pi$ bond is not formed to the $\mathrm{CF}_{2}$ group. Therefore, one would expect diradical intermediate 4 to be considerably lower in enthalpy than diradical 2. Our ab initio calculations found this expectation to be borne out, with $\mathbf{4}$ computed to be lower in enthalpy than 2 by $6.3 \mathrm{kcal} / \mathrm{mol} .{ }^{9}$
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However, a second expectation, that the TS connecting 1 to 4 should also be considerably lower in enthalpy than the TS connecting 1 to 2 , was proven to be incorrect by our calculations. The two TSs were computed to differ in enthalpy by only 1.1 $\mathrm{kcal} / \mathrm{mol} .{ }^{9}$ Subsequent kinetic studies by Dolbier and co-workers on the competing rearrangements of $\mathbf{6}$ to $\mathbf{7}$ and $\mathbf{8}$ found the free energy difference between the TSs leading to these two products to be $0.7 \mathrm{kcal} / \mathrm{mol}$ at $453{ }^{\circ} \mathrm{C},{ }^{11}$ in excellent agreement with the computational results.


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The calculations revealed that the highly pyramidalized $\mathrm{CF}_{2}$ group in diradical intermediate 4 is responsible for the higher than expected enthalpy of the TS connecting 1 to $4 .{ }^{9}$ The preferred pathway for the rearrangement of $\mathbf{1}$ to $\mathbf{5}$ is depicted in Scheme 1, which shows that ring opening of $\mathbf{1}$ occurs with inversion of the $\mathrm{CF}_{2}$ group, giving diradical 4 . Microscopic reversibility is preserved in the closure of $\mathbf{4}$ to 5 by facile rotation about the bond to the $\mathrm{CF}_{2}$ group in 4 , to form diradical $4^{\prime}$, which closes to $\mathbf{5}$, again with inversion of the configuration of the $\mathrm{CF}_{2}$ group.

Dolbier and co-workers have also found that introduction of a second $\mathrm{CF}_{2}$ group into the methylenecyclopropane ring results in the experimentally determined value of $E_{\mathrm{a}}=29.6 \mathrm{kcal} / \mathrm{mol}$ for rearrangement of 2,2,3,3-tetrafluoromethylenecyclopropane (9) to 1-(difluoromethylene)-2,2-difluoromethylenecyclopropane $(\mathbf{1 1})^{12}$ being $8.7 \mathrm{kcal} / \mathrm{mol}$ lower than $E_{\mathrm{a}}=38.3 \mathrm{kcal} / \mathrm{mol}$ for rearrangement of $\mathbf{1}$ to $\mathbf{3} .^{7}$ To try to understand why the introduction of a second $\mathrm{CF}_{2}$ group into the cyclopropane ring lowers $E_{\mathrm{a}}$ for methylenecyclopropane rearrangement by $6.7 \mathrm{kcal} /$ mol more than introduction of the first $\mathrm{CF}_{2}$ group, we have performed ab initio calculations on the rearrangement of 9 to 11.


Herein, we report the results of our study. We find that the presence of two $\mathrm{CF}_{2}$ groups destabilizes the cyclopropane ring of 9 , not only relative to the TS for ring opening, but also relative to the diradical intermediate (10) in the rearrangement and to

[^1]the product formed (11). Consequently, as conjectured by Dolbier and co-workers, ${ }^{12}$ the low $E_{\mathrm{a}}$ for rearrangement of $\mathbf{9}$ is due to destabilizing interactions between the vicinal $\mathrm{CF}_{2}$ groups in 9 , rather than to stabilization of the TS by the presence of two $\mathrm{CF}_{2}$ groups.

In addition to establishing the reason for the surprisingly low barrier to rearrangement of $\mathbf{9}$, our calculations also make the very interesting prediction of the existence of a $C_{2 v}$ intermediate, which may be regarded as a bond-stretch isomer of $9 .{ }^{13}$ Unlike the case in methylenecyclopropane $\mathbf{9}$, where the AOs that form the bond between the $\mathrm{CF}_{2}$ groups have their large lobes pointed toward each other, in the bond-stretch isomer of 9 the $\mathrm{CF}_{2}$ groups are inverted, so that the large lobes of these AOs are pointed away from each other. Consequently, direct closure of the bond-stretch isomer to $\mathbf{9}$ is calculated to have a high barrier, because this reaction requires simultaneous inversion of both of the highly pyramidalized $\mathrm{CF}_{2}$ groups in the bond-stretch isomer.

## Computational Methodology

Stationary points on the potential surface for the rearrangement of $\mathbf{9}$ to $\mathbf{1 1}$ were located by carrying out (4/4)CASSCF calculations with the $6-31 \mathrm{G}^{*}$ basis set. ${ }^{14}$ For 9 , the orbitals in the active space were comprised of the bonding and antibonding orbitals of the scissile $\sigma$ bond, as well as the $\pi$ and $\pi^{*}$ MOs. For other stationary points on the potential energy surface, the orbitals in the active space consisted of the four MOs, formed by the mixing of the $\sigma, \sigma^{*}, \pi$, and $\pi^{*}$ orbitals of 9 upon ring opening.

The geometries of the stationary points located are available as Supporting Information. ${ }^{15}$ At each stationary point, a (4/4)CASSCF vibrational analysis was performed to identify it as an energy minimum, a transition structure (TS), or a hill top, and to obtain the vibrational frequencies necessary to compute the enthalpy at 298 K . In addition, for each TS, the transition vector, found by the vibrational analysis, was used to follow the reaction pathway from the TS in both directions, to determine which pair of energy minima is connected by that TS. These calculations were performed with the Gaussian 03 suite of programs. ${ }^{16}$

To include the effects of dynamic electron correlation, ${ }^{17}$ single-point CASPT2 calculations ${ }^{18}$ were carried out at each (4/4)CASSCF stationary point. The CASPT2 calculations were not only performed with the $6-31 \mathrm{G}^{*}$ basis set, but also with the larger $6-311+\mathrm{G}(2 \mathrm{df}, 2 \mathrm{p})$ basis set. ${ }^{19}$ The CASPT2 calculations were carried out with the MOLCAS package of ab initio programs. ${ }^{20}$

## Results and Discussion

Pathways for Ring Opening of 2,2,3,3-Tetrafluoromethylenecyclopropane (9) to Diradical Intermediates 10 and 10'.
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Figure 1. Some of the (4/4)CASSCF/6-31G* stationary points on the potential surface for rearrangement of 2,2,3,3-tetrafluoro-methylenecyclopropane (9) to 1-(difluoromethylene)-2,2-difluorocyclopropane (11).

In analogy to the rearrangement of 2,2-difluoromethylenecyclopropane (1) to (difluoromethylene)cyclopropane (3) via the intermediacy of diradical (2) and to the crypto rearrangement of $\mathbf{1}$ to $\mathbf{5}$ via diradical $4,{ }^{9}$ the rearrangement of $\mathbf{9}$ to $\mathbf{1 1}$ is expected to occur via the intermediacy of diradical $\mathbf{1 0}$ and/or $\mathbf{1 0}^{\prime}$. We began our calculations by searching for the lowest energy pathway for the ring opening of $\mathbf{9}$ to $\mathbf{1 0}$.

Ring opening of 9 can occur, at least in principle, by three different pathways, involving disrotation, conrotation, or monorotation of the $\mathrm{CF}_{2}$ groups. We found that the disrotatory path leads to a transition structure (TS) in which the $\mathrm{CF}_{2}$ groups have rotated by $42.6^{\circ}$ and the $\mathrm{C} 2-\mathrm{C} 3$ bond has lengthened by $0.69 \AA$ from the equilibrium geometry of 9 . This TS (TS-12) is depicted in Figure 1, and Table 1 shows that TS-12 is computed to be $30.0 \mathrm{kcal} / \mathrm{mol}$ higher in enthalpy than 9 at the CASPT2/ $6-311+G(2 d f, 2 p)$ level of theory. ${ }^{21}$

From TS-12, continued disrotation of the $\mathrm{CF}_{2}$ groups by an additional $30.0^{\circ}$ leads to another TS (TS-13 in Figure 1), which is $4.3 \mathrm{kcal} / \mathrm{mol}$ lower than TS-12. In TS-13, the vibration with the imaginary frequency is no longer the $a^{\prime}$ disrotatory vibration of TS-12 but, instead, an $\mathrm{a}^{\prime \prime}$ vibration for symmetry-breaking conrotation of the $\mathrm{CF}_{2}$ groups. The point along the reaction coordinate at which the force constant for the $\mathrm{a}^{\prime \prime}$ vibration

[^2]Table 1. Relative Electronic Energies and Enthalpies (kcal/mol) of the Stationary Points on the Potential Surface for Rearrangement of 2,2,3,3-Tetrafluoromethylenecyclopropane (9) to 1-(Difluoromethylene)-2,2-difluorocyclopropane (11) a

|  | $6-31 G^{*}$ |  |  | $6-311+G(2 d f, 2 p)$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | CASSCF | CASPT2 |  | CASSCF | CASPT2 |
| $\mathbf{9}$ | 0 | 0 |  | 0 | 0 |
| 10 | $21.7(19.8)$ | $21.8(20.0)$ |  | $21.4(19.6)$ | $21.4(19.5)$ |
| $\mathbf{1 0}^{\prime}$ | $21.4(20.4)$ | $22.8(21.7)$ |  | $21.9(20.8)$ | $24.0(22.8)^{b}$ |
| TS (10/10') | $25.7(23.3)$ | $25.1(22.7)$ |  | $26.0(23.5)$ | $25.1(22.6)$ |
| 11 | $-4.8(-4.4)$ | $-8.6(-8.3)$ |  | $-4.9(-4.6)$ | $-9.2(-8.8)$ |
| TS-12 | $30.7(29.3)$ | $31.9(30.5)$ |  | $29.4(28.1)$ | $31.3(30.0)$ |
| TS-13 | $23.7(22.4)$ | $25.4(24.1)$ |  | $24.1(22.8)$ | $27.0(25.7)$ |
| TS-14 | $25.5(23.2)$ | $28.0(25.6)$ |  | $25.6(23.3)$ | $28.4(26.1)$ |
| 15 | $25.4(23.6)^{c}$ | $28.3(26.6)$ |  | $25.4(23.7)^{c}$ | $28.8(27.1)$ |
| TS-16 | $31.6(29.2)$ | $28.6(26.2)$ |  | $30.5(28.2)$ | $26.4(24.1)$ |
| TS-17 | $31.4(29.0)$ | $33.0(30.6)$ |  | $30.6(28.2)$ | $32.0(29.6)$ |
| 18 | $28.8(27.4)$ | $33.4(32.0)$ |  | $28.6(27.3)$ | $34.4(33.1)$ |
| 18-triplet | $27.6(26.4)$ | $32.0(30.8)$ |  | $27.5(26.3)$ | $33.1(31.9)$ |
| 19 | $30.4(28.5)$ | $35.1(33.2)$ |  | $30.1(28.2)$ | $36.1(34.1)$ |
| 19-triplet | $29.7(27.8)$ | $34.4(32.5)$ |  | $29.6(27.7)$ | $35.4(33.5)$ |
| 20 | $20.1(19.4)$ | $21.6(21.0)$ |  | $20.2(19.6)$ | $22.6(21.9)$ |
| 20-triplet | $28.3(27.2)$ | $32.7(31.5)$ |  | $28.5(27.4)$ | $34.2(33.1)$ |
| TS (20/9) | $44.8(41.6)$ | $39.9(36.7)$ |  | $42.5(39.3)$ | $36.8(33.6)$ |


#### Abstract

${ }^{a}$ Calculations were performed at $(4,4)$ CASSCF/6-31G* optimized geometries, and single-point CASSCF and CASPT2 energies were computed with both the $6-31 \mathrm{G}^{*}$ and the $6-311+\mathrm{G}(2 \mathrm{df}, 2 \mathrm{p})$ basis sets. ${ }^{b}$ Although the CASPT2 energy of $\mathbf{1 0}^{\prime}$ is lower than that of $\mathbf{T S}(\mathbf{1 0 / 1 0})$, the zero-point energy, associated with the one additional vibration that has a real frequency in $\mathbf{1 0}^{\prime}$, makes the CASPT2 enthalpy of $\mathbf{1 0}^{\prime}$ slightly higher than that of TS(10/ $\mathbf{1 0}^{\prime}$ ), which connects $\mathbf{1 0}$ to $\mathbf{1 0}$. ${ }^{c}$ Although the CASSCF energy of $\mathbf{1 5}$ is slightly lower than that of TS-14, the zero-point energy, associated with the one additional vibration that has a real frequency in $\mathbf{1 5}$, makes the CASSCF enthalpy of $\mathbf{1 5}$ higher than that of TS-14.


changes sign from positive at TS-12 to negative at TS-13 is called a valley-ridge inflection point. ${ }^{22}$
At the equivalent minima (10) that are connected by TS-13, one of the $\mathrm{CF}_{2}$ groups in TS $\mathbf{1 3}$ has become conjugated with the exocyclic double bond, and the other has rotated so that its singly occupied 2 p AO lies in the plane of the four carbon atoms. Thus, $\mathbf{1 3}$ is the $C_{s}$ TS for interchange of the pair of nonequivalent $\mathrm{CF}_{2}$ groups in intermediate $\mathbf{1 0} .{ }^{23}$

Table 1 shows that $\mathbf{1 0}$ is lower in enthalpy than TS-13 by $6.2 \mathrm{kcal} / \mathrm{mol}$, and the enthalpic barrier to reclosure of $\mathbf{1 0}$ to $\mathbf{9}$ via TS-12 is $10.5 \mathrm{kcal} / \mathrm{mol}$. The relative enthalpies of these and other important stationary points on the potential energy surface connecting 9 and $\mathbf{1 1}$ are indicated graphically in Figure 2.

We were unable to locate a true TS for conrotatory opening of 9 to 10 . Following a $C_{2}$ reaction path from 9 did, indeed, lead to a CASSCF energy maximum. This stationary point is higher in energy than TS-12 by 1.0 and $3.4 \mathrm{kcal} / \mathrm{mol}$ at,

[^3]

Figure 2. Schematic depiction of the relative CASPT2/6-311+G(2df, 2 p$)$ enthalpies of the stationary points along the pathway for the ring opening of 9 to diradical $\mathbf{1 0}$ and for the closure of $\mathbf{1 0}$ to $\mathbf{1 1}$ with inversion (via $\mathbf{1 5}$ ) or retention (via $\mathbf{1 0}$ ) of the configuration of the pyramidalized $\mathrm{CF}_{2}$ group in $\mathbf{1 0}$.
respectively, the (4/4)CASSCF/6-31G* and CASPT2/6-31G* levels of theory. However, a vibrational analysis found this $C_{2}$ energy maximum to have imaginary frequencies for both $a_{1}$ and $\mathrm{a}_{2}$ vibrations. Thus, this $C_{2}$ geometry is a mountain top on the global (4/4)CASSCF/6-31G* potential energy surface for rearrangement of 9 .

The fact that the $C_{2}$ conrotatory energy maximum is a mountain top suggests that there might be a true TS with no symmetry, in which ring opening of $\mathbf{9}$ to $\mathbf{1 0}$ occurs largely by rotation of just one $\mathrm{CF}_{2}$ group. However, all attempts to locate such a monorotatory TS led back to TS-12. Therefore, it appears that the preferred pathway for ring opening of $\mathbf{9}$ involves initial disrotation of both $\mathrm{CF}_{2}$ groups, passage over TS-12, followed by symmetry-breaking conrotation to form diradical intermediate 10. ${ }^{24}$

Ring opening of $\mathbf{9}$ to diradical $\mathbf{1 0}$ occurs with retention of configuration of the pyramidalized $\mathrm{CF}_{2}$ group that remains unconjugated with the double bond in $\mathbf{1 0}$. However, ring opening of $\mathbf{9}$ could, at least in principle, also lead to diradical $\mathbf{1 0}^{\prime}$, which differs from $\mathbf{9}$ and $\mathbf{1 0}$ by inversion of the configuration of the pyramidalized $\mathrm{CF}_{2}$ group.

At the CASSCF level, diradical $\mathbf{1 0}^{\prime}$ was found to have a $C_{1}$ equilibrium geometry, with the conjugated $\mathrm{CF}_{2}$ group pyramidalized by $43.2^{\circ}$. The CASSCF/6-31G* energy of this $C_{1}$ geometry is $0.9 \mathrm{kcal} / \mathrm{mol}$ lower than that of the $C_{s} \mathrm{TS}$, connecting $10^{\prime}$ to its mirror image, which has the conjugated $\mathrm{CF}_{2}$ group pyramidalized in the opposite direction. However, CASPT2/6-311 $+\mathrm{G}(2 \mathrm{df}, 2 \mathrm{p})$ calculations found the energies of the $C_{1}$ and $C_{s}$ geometries of $\mathbf{1 0}^{\prime}$ to be essentially the same. Presumably, the proximity of the fluorines on the non-conjugated $\mathrm{CF}_{2}$ group to one of the vinylic fluorines in $\mathbf{1 0}^{\prime}$ is responsible for $\mathbf{1 0}$ ' being computed to be $2.6 \mathrm{kcal} / \mathrm{mol}$ higher in energy than 10.

We were unable to find a low-energy TS for ring opening of 9 directly to $\mathbf{1 0}^{\prime}$ with inversion of configuration of the non-
(24) TS-12 for ring opening of $\mathbf{9}$ is similar to the TS for the ring opening of $\mathbf{1}$ to $4^{\prime}$ with retention of $\mathrm{CF}_{2}$ configuration. ${ }^{9}$ To reach the latter TS, the $\mathrm{CH}_{2}$ and $\mathrm{CF}_{2}$ groups in $\mathbf{1}$, like the $\mathrm{CF}_{2}$ groups in the ring opening of 9 , initially rotate in opposite directions.
conjugated $\mathrm{CF}_{2}$ group (vide infra). However, following ring opening of 9 to $\mathbf{1 0}$, there are several possible pathways for interconversion of $\mathbf{1 0}$ and $\mathbf{1 0}^{\prime}$. The pathway of lowest energy was calculated to be the one that involves rotation about the $\mathrm{C}-\mathrm{C}$ bond to the non-conjugated $\mathrm{CF}_{2}$ group. The CASPT2 energy of the $\operatorname{TS}\left[\mathbf{T S}\left(\mathbf{1 0} / \mathbf{1 0}^{\prime}\right)\right.$ along this pathway] is computed to be $1.1 \mathrm{kcal} / \mathrm{mol}$ greater than that of $\mathbf{1 0}^{\prime}$. However, because $\mathbf{1 0}^{\prime}$ has one more vibration with a real frequency than does TS( $\mathbf{1 0} / \mathbf{1 0}$ '), the CASPT2 enthalpy of $\mathbf{1 0}^{\prime}$ is actually computed to be $0.2 \mathrm{kcal} / \mathrm{mol}$ greater than that of $\mathbf{T S}\left(\mathbf{1 0} / \mathbf{1 0} \mathbf{0}^{\prime}\right)$.

A higher energy pathway for interconversion of $\mathbf{1 0}$ and $\mathbf{1 0}^{\prime}$ involves inversion of the non-conjugated $\mathrm{CF}_{2}$ group. The CASPT2 barrier to transformation of $\mathbf{1 0}$ to $\mathbf{1 0}^{\prime}$ by $\mathrm{CF}_{2}$ inversion is calculated to be $8.2 \mathrm{kcal} / \mathrm{mol}$, which is $5.1 \mathrm{kcal} / \mathrm{mol}$ greater than the barrier for formation of $\mathbf{1 0}^{\prime}$ from $\mathbf{1 0}$ by rotation of the non-conjugated $\mathrm{CF}_{2}$ group.

Ring Closure of 10 and $10^{\prime}$ to 1-(Difluoromethylene)-2,2difluorocyclopropane (11). Although diradical $\mathbf{1 0}^{\prime}$ is computed to be higher in enthalpy than diradical 10 by $3.3 \mathrm{kcal} / \mathrm{mol}$ at the CASPT2 level of theory, if the TS for ring closure of $\mathbf{1 0}^{\prime}$ were lower in energy than the TS for ring closure of $\mathbf{1 0}, \mathbf{1 0}^{\prime}$ could still lie on the lowest energy reaction pathway for rearrangement of $\mathbf{9}$ to $\mathbf{1 1}$.

Ring closure of $\mathbf{1 0}$ to $\mathbf{1 1}$ inverts the configuration of the nonconjugated $\mathrm{CF}_{2}$ group, whereas ring closure of $\mathbf{1 0}^{\prime}$ to $\mathbf{1 1}$ occurs with retention of $\mathrm{CF}_{2}$ configuration. Given the $8.2 \mathrm{kcal} / \mathrm{mol}$ CASPT2 energy barrier computed for inversion of the $\mathrm{CF}_{2}$ group in forming $\mathbf{1 0}^{\prime}$ from 10, it might have been imagined that ring closure of $\mathbf{1 0}^{\prime}$ with retention of $\mathrm{CF}_{2}$ configuration would have a lower barrier than ring closure of $\mathbf{1 0}$ with inversion. However, this was not found to be the case. Instead, as in the crypto methylenecyclopropane rearrangement of $\mathbf{1}$ to $\mathbf{5}$, where inversion of the $\mathrm{CF}_{2}$ group was calculated to be the preferred pathway for ring opening of $\mathbf{1}$ and ring closure to $\mathbf{5},{ }^{9}$ the TS for closure of $\mathbf{1 0}$ to $\mathbf{1 1}$ was computed to be lower than the TS for closure of $\mathbf{1 0}^{\prime}$ to $\mathbf{1 1}$.

As in the ring closure of $\mathbf{4}^{\prime}$ to 5 with inversion of $\mathrm{CF}_{2}$ configuration, CASSCF calculations find ring closure of $\mathbf{1 0}$ to 11 to involve passage over a TS (TS-14) to form a second
diradical intermediate (15), which has nearly the same CASSCF energy as TS-14. As shown in Figure 1, in $\mathbf{1 5}$ the $\mathrm{CH}_{2}$ and $\mathrm{CF}_{2}$ groups are aligned for $\sigma$ bond formation. Nevertheless, ring closure of $\mathbf{1 5}$ to $\mathbf{1 1}$ requires inversion of the $\mathrm{CF}_{2}$ group, and, at the CASSCF/6-311+G(2df,2p) level of theory, ring closure is prevented by a $4.5 \mathrm{kcal} / \mathrm{mol}$ barrier to passage over TS-16.

However, inclusion of dynamic electron correlation has a large effect on lowering the barrier to $\mathrm{CF}_{2}$ group inversion. ${ }^{9,25}$ Consequently, at the CASPT2 level of theory, the energy of TS-16 is actually $2.4 \mathrm{kcal} / \mathrm{mol}$ lower than that of $\mathbf{1 5}$ (Table 1 ).

The CASPT2 enthalpy of TS-14 for ring closure of $\mathbf{1 0}$ to $\mathbf{1 1}$ with inversion of $\mathrm{CF}_{2}$ configuration is calculated to be $3.5 \mathrm{kcal} /$ mol lower than the CASPT2 enthalpy of TS-17 for ring closure of $\mathbf{1 0}$ ' to $\mathbf{1 1}$ with retention of the $\mathrm{CF}_{2}$ group configuration. This enthalpy difference between the TSs for ring closure with, respectively, inversion and retention of configuration is about the same size as the CASPT2/6-31G* energy difference between these two types of TSs in the crypto methylenecyclopropane rearrangement of $\mathbf{1}$ to $\mathbf{5}$. As discussed previously for the latter rearrangement, ${ }^{9}$ in the rearrangement of $\mathbf{9}$ to $\mathbf{1 1}$ ring closure with inversion of the configuration of the highly pyramidalized $\mathrm{CF}_{2}$ group is favored over ring closure with retention by better overlap between the singly occupied AOs on the $\mathrm{CF}_{2}$ and $\mathrm{CH}_{2}$ groups in the TS for ring closure.

Reaction Thermochemistry. As shown graphically in Figure 2, our calculations find that the highest energy TS along the lowest energy pathway for the rearrangement of 9 to $\mathbf{1 1}$ is TS12, which connects 9 to diradical intermediate 10. The CASPT2 activation enthalpy of $E_{\mathrm{a}}=\Delta H^{\ddagger}+R T=30.0+0.8=30.8$ $\mathrm{kcal} / \mathrm{mol}$ for passage over this TS is in very good agreement with the value of $E_{\mathrm{a}}=29.6 \pm 1 \mathrm{kcal} / \mathrm{mol}$ measured by Dolbier and co-workers in the temperature range $150-160{ }^{\circ} \mathrm{C} .{ }^{12}$

As noted in the introduction, $E_{\mathrm{a}}=29.6 \mathrm{kcal} / \mathrm{mol}$ for the rearrangement of $\mathbf{9}$ to $\mathbf{1 1}$ is much smaller than expected. Based on the effect of the $\mathrm{CF}_{2}$ group in $\mathbf{1}$ on making $E_{\mathrm{a}}=38.3 \mathrm{kcal} /$ mol for rearrangement of $\mathbf{1}$ to $\mathbf{3}^{7}$ only $2 \mathrm{kcal} / \mathrm{mol}$ smaller than the $E_{\mathrm{a}}$ for rearrangement of the methyl-labeled hydrocarbon, ${ }^{8}$ substituent-effect additivity would have predicted $E_{\mathrm{a}} \approx 36 \mathrm{kcal} /$ mol for the rearrangement of $\mathbf{9}$ to 11. Thus, the effect of the pair of $\mathrm{CF}_{2}$ groups in $\mathbf{9}$ on lowering the barrier to rearrangement to $\mathbf{1 1}$ is ca. $6-7 \mathrm{kcal} / \mathrm{mol}$ larger than that expected from additivity.

Dolbier and co-workers conjectured that this additional reduction in the lowering of $E_{\mathrm{a}}$ for the rearrangement of 9 to $\mathbf{1 1}$ is due to destabilization of $\mathbf{9}$ by unfavorable interactions between the $\mathrm{CF}_{2}$ groups. ${ }^{12}$ If this were the case, the rearrangement of 9 to $\mathbf{1 1}$ should be more exothermic by $6-7 \mathrm{kcal} / \mathrm{mol}$ than the value of $\Delta H=-1.9 \mathrm{kcal} / \mathrm{mol}$ that was both measured ${ }^{7}$ and calculated ${ }^{9}$ for the rearrangement of $\mathbf{1}$ to $\mathbf{3}$.

Unfortunately, so little 9 was present at equilibrium that Dolbier and co-workers were unable to measure $\Delta H$ for the transformation of $\mathbf{9}$ into $\mathbf{1 1} .{ }^{12}$ However, we have calculated this enthalpy change, to see how it compares with the value of $\Delta H$ $\approx 8-9 \mathrm{kcal} / \mathrm{mol}$ that is expected, if repulsions between the $\mathrm{CF}_{2}$ groups in 9 are wholly responsible for making the $E_{\mathrm{a}}$ for rearrangement of 9 to $\mathbf{1 1} 6-7 \mathrm{kcal} / \mathrm{mol}$ lower than predicted by substituent additivity. As shown in Table 1, our CASPT2

[^4]calculations do indeed find $\Delta H=-8.3$ with the $6-31 \mathrm{G}^{*}$ basis set and $\Delta H=-8.8 \mathrm{kcal} / \mathrm{mol}$ with the $6-311+\mathrm{G}(2 \mathrm{df}, 2 \mathrm{p})$ basis set for the transformation of $\mathbf{9}$ into $\mathbf{1 1}$.

The difference between the enthalpies of the rearrangements of $\mathbf{1}$ to $\mathbf{3}$ and $\mathbf{9}$ to $\mathbf{1 1}$ is given by the isodesmic reaction in eq 1. We have confirmed that the CASPT2/6-31G* value of $\Delta H$


1

11


3


9
$=6.4 \mathrm{kcal} / \mathrm{mol}$ for the reaction in eq $1^{26}$ is, indeed, due to repulsions between the $\mathrm{CF}_{2}$ groups in 9 . To do so, we computed the enthalpy of the disproportionation reaction in eq 2 , which gives the enthalpy difference between having a pair of $\mathrm{CF}_{2}$ groups in the same methylenecyclopropane ring, as in $\mathbf{9}$, or in
2


MCP

9
two different methylenecyclopropane rings, as in two molecules of $\mathbf{1}$. The calculated CASPT2/6-31G* enthalpy of the reaction in eq 2 is $\Delta H=7.0 \mathrm{kcal} / \mathrm{mol},{ }^{26}$ thus confirming the hypothesis of Dolbier and co-workers that the presence of two $\mathrm{CF}_{2}$ groups in the same methylenecyclopropane ring destabilizes $9 .{ }^{12}$

Subtracting eq 1 from eq 2 gives eq 3. The value of $\Delta H=$ $0.6 \mathrm{kcal} / \mathrm{mol}$ for eq 3 shows that having both $\mathrm{CF}_{2}$ groups in the

same molecule is also destabilizing for rearrangement product 11, but by much less than for reactant 9 .

[^5]Disproportionation reactions, similar to those in eqs 2 and 3, can be used to assess the effect of having a pair of $\mathrm{CF}_{2}$ groups in diradical intermediate $\mathbf{1 0}$ and in the TS for ring opening of 9 to 10. Using the CASPT2/6-31G* results from ref 9 and from Table $1,{ }^{26}$ the enthalpy of $\Delta H=0.3 \mathrm{kcal} / \mathrm{mol}$ for the reaction in eq 4 shows that, as in rearrangement product 11, having both

$\mathrm{CF}_{2}$ groups in diradical intermediate $\mathbf{1 0}$ results in an almost negligible amount of destabilization.

In contrast, if the four diradical intermediates in eq 4 are replaced by the four TSs that connect the diradicals to the reactants, then CASPT2/6-31G* calculation of the enthalpy of the reaction in eq 5 finds that the presence of both $\mathrm{CF}_{2}$ groups in TS-12 destabilizes this TS to the extent of $3.7 \mathrm{kcal} / \mathrm{mol} .{ }^{27}$

$$
\begin{align*}
\mathrm{TS}(\mathbf{1} \rightarrow \mathbf{2})+\mathrm{TS}(\mathbf{1} \rightarrow \mathbf{4}) \rightarrow \\
\mathrm{TS}(\mathbf{M C P} \rightarrow \mathbf{T M M})+\mathbf{T S}-12 \tag{5}
\end{align*}
$$

It is tempting to attribute this destabilization to a residuum of the interaction between the $\mathrm{CF}_{2}$ groups, which destabilizes reactant 9 by $\Delta H=7.0 \mathrm{kcal} / \mathrm{mol}$ at the CASPT2/6-31G* level of theory. ${ }^{26}$ However, the lengthening of the bond between the $\mathrm{CF}_{2}$ groups, from $1.529 \AA$ in 9 to $2.154 \AA$ in TS-12, makes it not unreasonable to suppose that most of the repulsive interactions between the $\mathrm{CF}_{2}$ groups in $\mathbf{9}$ are absent from TS-12 or at least significantly reduced.

There is computational evidence that it is the stereochemistry, imposed on TS-12 by the presence of two $\mathrm{CF}_{2}$ groups, which is largely responsible for the destabilization of this TS. As already noted, TS-12 for the ring opening of 9 retains the configuration of both $\mathrm{CF}_{2}$ groups, because the TS for inverting one of them is quite high in energy (vide infra). In contrast, the TS that connects $\mathbf{1}$ to $\mathbf{4}$ maximizes overlap between the AOs of the $\mathrm{CH}_{2}$ and $\mathrm{CF}_{2}$ groups by inverting the configuration of the $\mathrm{CF}_{2}$ group. The CASPT2/6-31G* enthalpy of the TS that connects 1 to $4^{\prime}$, with retention of the configuration of the $\mathrm{CF}_{2}$ group, is $3.1 \mathrm{kcal} / \mathrm{mol}$ higher than the TS that connects $\mathbf{1}$ to $\mathbf{4}$ by inverting the $\mathrm{CF}_{2}$ group. ${ }^{9}$ Therefore, it can be argued that the major factor in the destabilization of TS-12 is the necessity
(27) This means that the expected value of $\Delta H^{\ddagger}$ for the rearrangement of 9 to 11 is only $7.0-3.7=3.3 \mathrm{kcal} / \mathrm{mol}$ higher than the CASPT $2 / 6-31 \mathrm{G}^{*}$ value of $\Delta H^{\ddagger}=30.5 \mathrm{kcal} / \mathrm{mol}$ that is actually calculated. Using the experimental $E_{\mathrm{a}}$ values, ${ }^{8}$ including an estimate of $\Delta E_{\mathrm{a}}=0.7 \mathrm{kcal} / \mathrm{mol}$ between the formation of 7 and $\mathbf{8}$ from $6,{ }^{11} E_{\mathrm{a}}=38.3-1.9-0.7=35.7 \mathrm{kcal} / \mathrm{mol}$ is expected for $\mathbf{9} \rightarrow \mathbf{1 1}$, which is $6.1 \mathrm{kcal} / \mathrm{mol}$ higher than the value of $E_{\mathrm{a}}=$ $29.6 \pm 1.0 \mathrm{kcal} / \mathrm{mol}$ actually measured. ${ }^{10}$ The major contributor to the 6.1 $-3.3=2.8 \mathrm{kcal} / \mathrm{mol}$ difference between the measured and calculated deviations from substituent-effect additivity in the rearrangement of $9 \rightarrow$ 11 is the fact that the value of $E_{\mathrm{a}}=29.6 \pm 1.0 \mathrm{kcal} / \mathrm{mol}$, measured by Dolbier and co-workers for this reaction, is $1.7 \mathrm{kcal} / \mathrm{mol}$ lower than the CASPT2/6-31G* value of $E_{\mathrm{a}}=30.5+0.8=31.3 \mathrm{kcal} / \mathrm{mol}$.
for 9 to undergo ring opening with retention of configuraton of both $\mathrm{CF}_{2}$ groups.

Why Is 9 Destabilized? The near-zero enthalpies computed for the reactions in eqs 3 and 4 indicate that the CASPT2/6$31 \mathrm{G}^{*}$ value of $\Delta H=7.0 \mathrm{kcal} / \mathrm{mol}$ that is computed for the reaction in eq $2^{26}$ must have its origin either in the proximity of the $\mathrm{CF}_{2}$ groups in $\mathbf{9}$ or in their cooperative destabilization of the three-membered ring of $\mathbf{9}$. To test which of these two hypotheses is correct, we carried out MP2 calculations on the disproportionation reaction for the acyclic compounds in eq 6.

$$
\begin{align*}
& 2 \mathrm{H}_{3} \mathrm{C}-\mathrm{CF}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{3} \rightarrow \\
& \quad \mathrm{H}_{3} \mathrm{C}-\mathrm{CF}_{2}-\mathrm{CF}_{2}-\mathrm{CH}_{3}+\mathrm{H}_{3} \mathrm{C}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{3} \tag{6}
\end{align*}
$$

With the $6-31 \mathrm{G}^{*}$ basis set, this reaction was computed to be endothermic by $5.9 \mathrm{kcal} / \mathrm{mol} .{ }^{28 \mathrm{a}, 30}$ Because this value is only $1.1 \mathrm{kcal} / \mathrm{mol}$ less than that computed for the disproportionation reaction in eq 2 , it would appear that the proximity of the $\mathrm{CF}_{2}$ groups in 9, rather than their presence in the same threemembered ring, is largely responsible for the endothermicity of the reaction in eq 2 .

However, the $\mathrm{C}-\mathrm{H}$ and $\mathrm{C}-\mathrm{F}$ bonds at C 2 and C 3 of $\mathbf{M C P}$, 3, and $\mathbf{9}$ in eq 2 are eclipsed, whereas those of the butanes in eq 6 are staggered. ${ }^{33}$ Therefore, we repeated the calculation of the enthalpy of the reaction in eq 6 , but with the butanes each constrained to an eclipsed conformation with the methyl groups syn to each other. With the $\mathrm{C}-\mathrm{H}$ and $\mathrm{C}-\mathrm{F}$ bonds at C 2 and C3 of the butanes forced to be eclipsed, the reaction in eq 6 is computed to be endothermic by $11.2 \mathrm{kcal} / \mathrm{mol}$ at the MP2/631G* level of theory. ${ }^{28 b}$

By computing the enthalpy change for anti to syn isomerization of each of the molecules in eq 6, it is easy to show that, when the butanes are constrained to the syn conformation, the $5.3 \mathrm{kcal} / \mathrm{mol}$ larger endothermicity of eq 6 is due to the large increase in destabilizing interactions in 2,2,3,3-tetrafluorobutane. The MP2/6-31G* enthalpy increases for anti to syn isomeriza-
(28) The following results were obtained at the MP2/6-311+G(2df,2p) level: (a) The reaction in eq 6 was computed to be endothermic by $6.5 \mathrm{kcal} / \mathrm{mol}$, and by $6.4 \mathrm{kcal} / \mathrm{mol}$ at the G3 level of theory. ${ }^{29}$ (b) With the butanes each constrained to have a syn geometry, the enthalpy of the reaction in eq 6 was computed to be $12.7 \mathrm{kcal} / \mathrm{mol}$. (c) The enthalpy changes for anti $\rightarrow$ syn in butane, 2,2-difluorobutane, and 2,2,3,3-tetrafluorobutane were calculated to be, respectively, $5.5,4.3$, and $9.3 \mathrm{kcal} / \mathrm{mol}$.
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tion are $5.8 \mathrm{kcal} / \mathrm{mol}$ for butane, $5.3 \mathrm{kcal} / \mathrm{mol}$ for 2,2 -difluorobutane, and $10.1 \mathrm{kcal} / \mathrm{mol}$ for $2,2,3,3$-tetrafluorobutane. ${ }^{28 \mathrm{c}}$ The increase in the enthalpy of 2,2,3,3-tetrafluorobutane is nearly twice as large as the increases for butane and 2,2-difluorobutane, presumably due to the much higher energetic cost of eclipsing between the pairs of $\mathrm{C}-\mathrm{F}$ bonds in 2,2,3,3-tetrafluorobutane.

In $\mathbf{9}$, as in syn-2,2,3,3-tetrafluorobutane, there are two pairs of eclipsed $\mathrm{C}-\mathrm{F}$ bonds. Nevertheless, the enthalpy of the disproportionation reaction in eq 2 is $4.2 \mathrm{kcal} / \mathrm{mol}$ smaller than that of the disproportionation reaction in eq 6 for the syn conformers of the butanes. The probable reason for the smaller endothermicity of the reaction in eq 2 is that the small internal angles at C 2 and C 3 of the three-membered ring in 9 result in a calculated distance of $2.837 \AA$ between eclipsed pairs of fluorines. This F-F distance in $\mathbf{9}$ is $0.434 \AA$ larger than that in the syn conformation of 2,2,3,3-tetrafluorobutane. Therefore, the repulsions between the eclipsed $\mathrm{C}-\mathrm{F}$ bonds are smaller in 9 than in syn-2,2,3,3-tetrafluorobutane.

Ring Opening of 9 without $\mathbf{C F}_{2}$ Rotations. As already noted, we were unable to locate a low-energy TS for ring opening of 9 with inversion of configuration of just one $\mathrm{CF}_{2}$ group. In $C_{s}$ symmetry, we were able to find a TS connecting 9 to a $C_{s}$ intermediate with one inverted $\mathrm{CF}_{2}$ group (18), but on the global potential surface both this $C_{s} \mathrm{TS}$ and $\mathbf{1 8}$ had an imaginary frequency for rotating the inverted $\mathrm{CF}_{2}$ group into conjugation with the $\pi$ bond to form $\mathbf{1 0}$. Thus, this $C_{s}$ TS is actually a mountain top on the global potential energy surface, and its energy is $6.2 \mathrm{kcal} / \mathrm{mol}$ higher in energy than TS-12 for ring opening of 9 with retention of configuration in both $\mathrm{CF}_{2}$ groups.


Nevertheless, our finding that $\mathbf{1 8}$ has a $3.1 \mathrm{kcal} / \mathrm{mol}$ barrier to ring closure to 9 led us to investigate whether $\mathbf{1 9}$ and $\mathbf{2 0}$ are also separated from 9 by barriers. At the (4/4)CASSCF/6-31G* level, we were, in fact, able to locate a shallow $C_{2 v}$ minimum, corresponding to $\mathbf{1 9}$, but $\mathbf{1 9}$ has imaginary frequencies for conand disrotation of the $\mathrm{CF}_{2}$ groups into conjugation with the double bond. The CASSCF barrier to ring closure of 19 directly to 9 is only $0.3 \mathrm{kcal} / \mathrm{mol}$, and at the CASPT2 level ring closure of $\mathbf{1 9}$ to 9 becomes barrierless.

The $\mathrm{CF}_{2}$ groups in $\mathbf{1 9}$ are, unlike those in $\mathbf{1 8}$, both pyramidalized in the same direction. However, as in 18, the singly occupied AOs in 19 are not well oriented for overlap. A measure of the degree to which singly occupied AOs interact through space in $\mathbf{1 8}$ and $\mathbf{1 9}$ is provided by the adiabatic energy differences between the lowest singlet and triplet states in these two diradicals. As shown in Table 1, in both diradicals the CASPT2 calculations actually find the triplet to be lower in energy than the singlet, by $1.2 \mathrm{kcal} / \mathrm{mol}$ in 18 and by $0.6 \mathrm{kcal} /$ mol in 19. Clearly, overlap between the singly occupied AOs in $\mathbf{1 8}$ and 19 is small.

Although the large lobes of the AOs on the $\mathrm{CF}_{2}$ groups in 20 are directed away from each other, as in [1.1.1]propellane, ${ }^{34}$ the favorable angular orientation of these $\mathrm{AOs}^{9}$ was expected
to provide more bonding in $\mathbf{2 0}$ than in $\mathbf{1 8}$ or $\mathbf{1 9}$. The fact that singlet $\mathbf{2 0}$ is calculated to be $11.2 \mathrm{kcal} / \mathrm{mol}$ lower in enthalpy than triplet 20 confirms this supposition. Table 1 shows that the CASPT2 enthalpy of $\mathbf{2 0}$ is also 11.2 and $12.2 \mathrm{kcal} / \mathrm{mol}$ lower than those of, respectively, $\mathbf{1 8}$ and $\mathbf{1 9}$ and only $2.4 \mathrm{kcal} / \mathrm{mol}$ higher than that of $\mathbf{1 0}$.

A vibrational analysis finds that, like $\mathbf{9}, \mathbf{2 0}$ is a true energy minimum on the global (4/4)CASSCF/6-31G* potential energy surface. The $\sigma$ bonding between the $\mathrm{CF}_{2}$ groups in $\mathbf{2 0}$ makes their rotation unfavorable, and the large barrier to $\mathrm{CF}_{2}$ group inversion makes ring closure of $\mathbf{2 0}$ directly to 9 energetically costly. In fact, the barrier to direct ring closure of 20 to 9 by simultaneous inversion of the configurations of both $\mathrm{CF}_{2}$ groups via $\mathbf{T S}(\mathbf{2 0} / 9)$ is calculated to be $11.7 \mathrm{kcal} / \mathrm{mol} .{ }^{35}$

Although simultaneous inversion of two isolated $\mathrm{CF}_{2}$ groups would require twice as much energy as their sequential inversion, inversion of just one $\mathrm{CF}_{2}$ group in $\mathbf{2 0}$, to form $\mathbf{1 8}$, sacrifices most of the bonding between the $\mathrm{CF}_{2}$ groups in 20. As a result, the enthalpy of the TS for ring closure of $\mathbf{2 0}$ to 9 via sequential inversion of the $\mathrm{CF}_{2}$ groups is calculated to be $2.6 \mathrm{kcal} / \mathrm{mol}$ higher than that of $\mathbf{T S}(\mathbf{2 0} / \mathbf{9})$ for ring closure of 20 directly to 9 , by simultaneous inversion of both $\mathrm{CF}_{2}$ groups.

However, the lowest energy pathway connecting 20 to 9 involves $\mathrm{CF}_{2}$ rotation, rather than inversion. Rotation of one $\mathrm{CF}_{2}$ group in $\mathbf{2 0}$ into conjugation with the double bond has a barrier of only $1.6 \mathrm{kcal} / \mathrm{mol}$ and leads to intermediate $\mathbf{1 0}^{\prime}$. Rotation of the non-conjugated $\mathrm{CF}_{2}$ group in $\mathbf{1 0}^{\prime}$ requires passage over a TS that is $1.1 \mathrm{kcal} / \mathrm{mol}$ higher in energy than $\mathbf{1 0}^{\prime}$, and leads to $\mathbf{1 0}$. From 10, closure to 9 can occur via passage over TS-12. This TS is $3.6 \mathrm{kcal} / \mathrm{mol}$ lower in enthalpy than $\mathbf{T S}(\mathbf{2 0 / 9})$ for closure of $\mathbf{2 0}$ directly to 9 with simultaneous inversion of both $\mathrm{CF}_{2}$ groups.

The existence of two energy minima, 9 and 20, both with $C_{2 v}$ symmetry and differing in the length of the $\mathrm{C}-\mathrm{C}$ bonds between the two $\mathrm{CF}_{2}$ groups ( $1.529 \AA$ in 9 and $2.490 \AA$ in $\mathbf{2 0}$ ), may be regarded as a rare example of bond-stretch isomerism. ${ }^{13}$ However, the relationship between 9 and 20 is unlike that between any of the other pairs of bond-stretch isomers that have been identified, experimentally or computationally. Bond-stretch isomers 9 and 20 differ in the direction of pyramidalization of the $\mathrm{CF}_{2}$ groups, toward each other in 9 and away from each other in 20. Direct interconversion of $\mathbf{9}$ and $\mathbf{2 0}$ is thus prevented by the large barrier to inversion of the configurations of two $\mathrm{CF}_{2}$ radical centers. ${ }^{35}$

We propose the name "bond-stretch invertomers" to describe the relationship between 9 and 20 and between other bondstretch isomers that are similarly related. Bond-stretch invertomers differ in the direction of pyramidilization of the two atoms that form a bond, so the members of a pair of bondstretch invertomers can be distinguished by whether the large lobes or the small lobes of the AOs on these atoms point toward each other. The existence of a pair of bond-stretch invertomers

[^6]requires that the overlap between the AOs in both geometries is strong enough and that the barrier to inversion of the pyramidalized atoms is high enough to make both geometries true energy minima.

## Conclusions

Our CASPT2 calculations give an energy of activation for the rearrangemernt of $\mathbf{9}$ to $\mathbf{1 1}$ that is in very good agreement with the value of $E_{\mathrm{a}}=29.6 \mathrm{kcal} / \mathrm{mol}$ measured by Dolbier and co-workers. ${ }^{12}$ Our calculations confirm Dolbier's conjecture, ${ }^{12}$ that the reason the $E_{\mathrm{a}}$ for rearrangement of $\mathbf{9}$ to $\mathbf{1 1}$ is $8.7 \mathrm{kcal} /$ mol lower than $E_{\mathrm{a}}=38.3 \mathrm{kcal} / \mathrm{mol}$ for rearrangement of $\mathbf{1}$ to $\mathbf{3}^{7}$ is destabilization of $\mathbf{9}$ by the pairs of eclipsed $\mathrm{CF}_{2}$ bonds at C 2 and C 3 of its cyclopropane ring, rather than stabilization of the TS for forming $\mathbf{1 1}$ from 9 .

Our calculations reveal that eclipsing is much more destabilizing for vicinal pairs of $\mathrm{C}-\mathrm{F}$ bonds than either for vicinal pairs of $\mathrm{C}-\mathrm{H}$ bonds or for $\mathrm{C}-\mathrm{F}$ bonds that are vicinal to $\mathrm{C}-\mathrm{H}$ bonds. However, the calculated enthalpy of the disproportionation reaction in eq 6 shows that, even in the lowest energy, staggered conformations, the interactions between the vicinal pairs of $\mathrm{C}-\mathrm{H}$ bonds in butane and the vicinal pairs of $\mathrm{C}-\mathrm{F}$ bonds 2,2,3,3-tetrafluorobutane are less favorable than the interactions between the vicinal $\mathrm{C}-\mathrm{H}$ and $\mathrm{C}-\mathrm{F}$ bonds in 2,2difluorobutane. ${ }^{30,33}$

Our CASPT2 calculations of the potential surface for rearrangement of $\mathbf{9}$ have identified 20, a bond-stretch isomer of $\mathbf{9}$, as a local minimum. These two isomers differ by inversion of both of the pyramidalized $\mathrm{CF}_{2}$ groups that form the unique $\mathrm{C}-\mathrm{C}$ bond in $\mathbf{9}$ and 20. In 9 , bonding occurs between the large "front" lobes of the hybridized AOs on the $\mathrm{CF}_{2}$ groups, whereas in $\mathbf{2 0}$ bonding involves the small "back" lobes of these AOs. We propose the name "bond-stretch invertomers" to describe the relationship between a pair of bond-stretch isomers that differ in this manner.

For a pair of bond-stretch invertomers both to be local minima, the overlap between the unique pair of AOs in both geometries must be strong enough to prevent rotation, and the barrier to inversion of the radicals that form the bond must be high enough to create a barrier to direct conversion of the higher to the lower energy bond-stretch invertomer. Molecules that contain pairs of atoms from the second row of the periodic table and beyond, where barriers to inversion of radical centers are higher than in the first row, ${ }^{36}$ are therefore good candidates for having pairs of bond-stretch invertomers. Whether this is in fact the case and whether the existence of bond-stretch invertomers will prove to be of chemical significance, rather than of purely theoretical interest, are both the subject of computational studies that are currently in progress.

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Supporting Information Available: Optimized geometries, energies, thermal corrections, and vibrational frequencies for all of the minima and TSs discussed in the text and references, and the complete list of authors for ref 16 . This material is available free of charge via the Internet at http://pubs.acs.org.

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[^2]:    (21) Unless otherwise noted, all of the enthalpies cited in the text were computed at the $(4 / 4)$ CASPT $2 / 6-311+G(2 \mathrm{df}, 2 \mathrm{p}) / /(4 / 4) \mathrm{CASSCF} / 6-31 \mathrm{G}^{*}$ level of theory.

[^3]:    (22) (a) Metiu, H.; Ross, J.; Silbey, R.; George, T. F. J. Chem. Phys. 1974, 61, 3200. (b) Valatazanos, P.; Ruedenberg, K. Theor. Chim. Acta 1986, 69, 281. For recent discussions of valley-ridge inflection points in connection with the ene reaction of singlet oxygen, see: (c) Singleton, D. A.; Hang, C.; Szymanski, M. J.; Meyer, M. P.; Leach, A. G.; Kuwata, K. T.; Chen, J. S.; Greer, A.; Foote, C. S.; Houk, K. N. J. Am. Chem. Soc. 2003, 125, 1319. (d) Gonzalez-Lafont, A.; Moreno, M.; Lluch, J. M. J. Am. Chem. Soc. 2004, 126, 13089.
    (23) We also located a $C_{2}$ intermediate that is connected by a pair of mirrorimage $C_{1}$ TSs to the two equivalent minima, corresponding to $\mathbf{1 0}$. The $C_{2}$ structure has (4/4)CASSCF energy that is only $0.1 \mathrm{kcal} / \mathrm{mol}$ lower than that for the pair of mirror-image $C_{1}$ structures, and, at the CASPT2/631G* level of theory, the $C_{2}$ structure is actually $0.2 \mathrm{kcal} / \mathrm{mol}$ above the pair of mirror-image $C_{1}$ structures. Therefore, it is probably correct to call the $C_{2}$ structure a TS for exchange of non-equivalent $\mathrm{CF}_{2}$ groups in $\mathbf{1 0}$. The CASPT2/6-31G* energy of this $C_{2}$ TS is actually $0.8 \mathrm{kcal} / \mathrm{mol}$ lower than that of the $C_{s}$ TS (TS-13) for $\mathrm{CF}_{2}$ exchange in 10. However, because the $C_{2}$ TS does not lie on the reaction coordinate for ring opening of 9 , it does not appear in Figure 1 or Table 1. Nevertheless, its geometry and CASSCF and CASPT2 enegies are given in the Supporting Information. ${ }^{15}$

[^4]:    (25) For examples, see: (a) Hrovat, D. A.; Sun, H.; Borden, W. T. THEOCHEM 1988, 163, 51. (b) Johnson, W. T. G.; Borden, W. T. J. Am. Chem. Soc. 1997, 119, 5930. (c) Skancke, P. N.; Hrovat, D. A.; Borden, W. T. J. Phys. Chem. A 1999, 103, 4043.

[^5]:    (26) CASPT2/6-31G* enthalpies for $\mathbf{9 - 1 2}$ were used, so that they could be compared with the CASPT2/6-31G* enthalpies for $\mathbf{1 - 5}$ that we had previously computed. ${ }^{9}$ However, we have confirmed that the CASPT2/6$31 G^{*}$ enthalpy changes, given in the text, for the reactions in eqs $1-3$ differ by, at most, only a few tenths of a $\mathrm{kcal} / \mathrm{mol}$ from the CASPT2/6$311+\mathrm{G}(2 \mathrm{df}, 2 \mathrm{p})$ values of, respectively, $6.6,7.2$, and $0.6 \mathrm{kcal} / \mathrm{mol}$ for these three reactions.

[^6]:    (34) Review: Wiberg, K. B. Chem. Rev. 1989, 89, 975.
    (35) It should be noted that in the ring closure of $\mathbf{1 0}$ to $\mathbf{1 1}$ (and of $\mathbf{4}^{\prime}$ to 5 ), ${ }^{9}$ the existence of an intermediate (15), which is analogous to $\mathbf{2 0}$, is predicted at the CASSCF level of theory. However, ring closure of $\mathbf{1 5}$ to $\mathbf{1 1}$ via TS-16 requires inversion of only one $\mathrm{CF}_{2}$ group, whereas ring closure of $\mathbf{2 0}$ to 9 via TS(20/9) requires inversion of both $\mathrm{CF}_{2}$ groups. Consequently, the CASSCF barrier to ring closure of $4.5 \mathrm{kcal} / \mathrm{mol}$ for passage over TS-16 is much smaller than that of $19.7 \mathrm{kcal} / \mathrm{mol}$ for passage over $\mathbf{T S}(\mathbf{2 0} / \mathbf{9})$. In addition, with inclusion of dynamic electron correlation, the CASPT2 barrier to passage over TS-16 vanishes, but the CASPT2 barrier of $11.7 \mathrm{kcal} / \mathrm{mol}$ for passage over TS(20/9) remains substantial.

[^7]:    (36) Review: Kutzelnigg, W. Angew. Chem., Int. Ed. Engl. 1984, 23, 272.

